

IMPROVED PERFORMANCE OF THE V-BLAST SYSTEM BY MODIFYING THE CHANNEL MATRIX

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Abstract - MIMO system (multiple antennas at the transmitter and receiver) is capable of very high theoretical capacities. As an important space-time code, V-BLAST (Vertical-Bell Lab Layered Space-Time) code has been researched recently. The critical research topics of V-BLAST system are to reduce the complexity and to increase the system performance. In this paper, we investigate the effect of modified channel matrix on the system performance. Two nulling criterions Zero-Forcing (ZF) and Minimum Mean Square Error (MMSE) are analyzed. We also perform simulation to verify the analysis.

Index Terms – V-BLAST, MIMO, Zero-Forcing and MMSE detection, wireless communication.

I. INTRODUCTION

It has been shown in recent research that the deployment of multiple antennas on both sides of a transmitter and receiver provides a larger capacity increase compared to single antennas systems [1], [2], [3]. A multiple-input multiple-output (MIMO) system that employs this trend is the V-BLAST (Vertical Bell Labs Layered Space-Time) architecture proposed in [3]. The structure is designed as a vertically layered coding, where independent code streams (called layers) are assigned with a certain transmit antenna. At the receiver, one way to execute the detection for this system is to use conventional adaptive antenna array (AAA) techniques [3], i.e. linear combination nulling. Nulling is carried out by linearly weighting the received signals in order to meet some relevant performance standard, such as zero-forcing (ZF) or minimum mean square error (MMSE). Zero-forcing was first proposed in [1]. However due to the limitation of pseudo inverse matrix computation when the number of antennas increases, zero-forcing seemed not feasible for real time implementation. To remarkably reduce the computational complexity, a very efficient method utilizing the QR and optimal detection order QR decomposition (called ZF-SQRD) of the channel matrix was proposed in [4]. The problem of noise enhancement through zero-forcing and QR decomposition has been paid attention

to. A significant improvement can clearly be seen by including the noise term in the design of the linear weighting vector. This can be done by MMSE detection schemes, where we can trade off between noise and interference proposed in [4] and by introducing a lower complexity in [7]. An extension of the ZF-SQRD algorithm to the MMSE solution called MMSE-SQRD was introduced in [6].

In this paper, we propose a modification of the channel matrix in MMSE criterion. After detecting the sub-stream, channel matrix will be deflated by zeroing the corresponding column. This is because in MMSE the received vector is not nulled completely. In every detection step, there still remains the interference. In order to minimize as much interference as possible the corresponding channel matrix must be modified, i.e. corresponding column is zeroed, so that the detected sub-stream will not appear in the receive vector. Otherwise, wrongly detected sub-stream will increase the interference for the next step.

The remainder of this paper is organized as follows. In Section II, the system overview is introduced. In section III, ZF and MMSE are reviewed. The effect of the modification of channel matrix is investigated in Section IV. The results are compared in Section V and concluding remark can be seen in Section VI.

II. SYSTEM OVERVIEW

The system is considered with n_T transmit and $n_R \geq n_T$ receive antennas. The data is demultiplexed in n_T data sub-streams of equal length (called layers). These sub-streams are mapped into M-PSK or M-QAM symbols t_1, t_2, \dots, t_{n_T} and simultaneously transmitted over n_T antennas. Furthermore, we can use a forward error correction code to encode the data sub-streams before mapping. However, it is not addressed in this paper. We will investigate the application under assumption uncoded symbols.

In order to outline the V-BLAST system, one time slot of the time-discrete complex base band model is

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examined. Let¹ $t = [t_1, t_2, \dots, t_{n_T}]^T$ defines the $n_T \times 1$ vector of transmit symbols, then the corresponding

¹ In this paper, $(\cdot)^T$ and $(\cdot)^H$ represents for the matrix transposition and Hermitian transposition, in that order. I_a denotes the $a \times a$ identity matrix

$n_R \times 1$ vector of receive symbols $r = [r_1, r_2, \dots, r_{n_R}]^T$ is given by

$$r = Ht + n \quad (1)$$

In (1), $n = [n_1, n_2, \dots, n_{n_R}]^T$ stands for the white Gaussian noise of variance σ_n^2 observed at the n_R receive antennas while the average transmit power of each antenna is normalized to one i.e. $E\{tt^H\} = I_{n_T}$ and $E\{nn^H\} = \sigma_n^2 I_{n_R}$

The $n_R \times n_T$ channel matrix H

$$H = \begin{pmatrix} h_{1,1} & \dots & h_{1,n_T} \\ \vdots & \ddots & \vdots \\ h_{n_R,1} & \dots & h_{n_R,n_T} \end{pmatrix} \quad (2)$$

includes i.i.d complex fading gains $h_{j,i}$ expressing the tap gains between transmit antenna i and receive antenna j with unit variance. We presume a flat fading environment, in which the channel matrix H is constant over a frame and changes independently from frame to frame (block fading channel). The distinct gains are assumed to be uncorrelated and are perfectly known in the receiver side

III. V-BLAST DETECTION

In this section, both ZF and MMSE criterion in V-BLAST architecture are reviewed. Two major operations are used: nulling and cancellation. With nulling, each sub-stream is regarded as the desired signal and the remaining is considered as interferes.

At each detecting step, all undesired sub-streams are nulled by linearly weighting the receive vector r . In the literature, ZF and MMSE criterions are widely deployed. The decision statistic y_i of the i -th sub-stream is calculated by multiplying the i -th row of the decorrelating matrix D with the receive vector, given by:

$$y_i = (D)_i r \quad (3)$$

where $(D)_i$ represents the i -th row of matrix D corresponding to the criterion in use.

To attain better performance, nulling always comes together with cancellation. At every detecting step, after the decision the generated version is cancelled from the received signal before moving on to the next stage.

A. Zero-Forcing Detection

The receive vector r is multiplied with a filter matrix D . Zero-forcing points out that the mutual interference between all layers will be completely suppressed. This can be achieved by the Moore-Penrose pseudo-inverse (defined by $(\cdot)^+$) of the channel matrix

$$D_{ZF} = H^+ = (H^H H)^{-1} H^H \quad (4)$$

The receive vector is linearly weighted with the nulling vector $(D)_i$ and the result

$$y_i = (D)_i r = (D)_i (Ht + n) = t_i + \tilde{n}_i \quad (5)$$

y_i is considered as the decision statistic for the i -th sub-stream and $\tilde{n}_i = (D)_i n$ is the noise enhancement. By using the quantization operation $Q[\cdot]$ appropriately, the i -th sub-stream can be estimated likely

$$\hat{t}_i = Q[y_i] \quad (6)$$

A successive interference cancellation technique based on the ZF criterion was proposed in [2]. In this scheme, the signals are not detected in parallel, but one after another. The interference caused by the detected signal \hat{t}_i is now extracted from the receive signal vector r_i

$$r_{i+1} = r_i - (H)_i \hat{t}_i \quad (7)$$

where $(H)_i$ is i -th column of the channel matrix.

When symbol cancellation is deployed, the order detection becomes very important to the entire performance of the system. Let the order set $S = \{k_1, k_2, \dots, k_{n_T}\}$ be a permutation of the integers $1, 2, \dots, n_T$ to specify the detection sequence. Thus the values $y_{k_1}, y_{k_2}, \dots, y_{k_{n_T}}$ are filtered one by one, the transmit signals $\hat{t}_{k_1}, \hat{t}_{k_2}, \dots, \hat{t}_{k_{n_T}}$ are estimated and the interference is cancelled out step by step according to equations (5) and (7). In order to obtain the minimum error probability, the optimal order is used. The sub-stream which has the largest post detection signal-to-noise ratio is detected first:

$$(SNR)_{k_i} = \frac{E\{|t_{k_i}|^2\}}{E\{|n_{k_i}|^2\} \|(D)_{k_i}\|^2} \sim \frac{1}{\|(D)_{k_i}\|^2} \quad (8)$$

$\langle \cdot \rangle$ denotes the expectation over the constellation set. $|\cdot|$ and $\|\cdot\|$ denote the complex amplitude and the vector norm respectively. Consequently, we

choose the row k_i -th $(D)_{k_i}$ of decorrelating matrix D with minimum norm and hence detect the corresponding sub-stream t_{k_i}

B. Minimum Mean Square Error

In [5] the decorrelating matrix D in the MMSE criterion is chosen to expose the solution for minimizing the problem of this below metric

$$E[\|t - Dr\|^2] = H^H (HH^H + \sigma_n^2 I_{nR})^{-1} \quad (9)$$

The decorrelating matrix is then given by $D = H^H (HH^H + \sigma_n^2 I_{nR})^{-1}$ (10)

The optimal order is chosen such that the $(SNR)_{k_i}$ after combining the k_i -th sub-stream to be detected at each stage is maximized

$$(SNR)_{k_i} = \frac{\|(D)_{k_i} (H)_{k_i}\|^2 < |t_{k_i}|^2 >}{\sigma_n^2 \|(D)_{k_i}\|^2} \quad (10)$$

where $(D)_{k_i}$ is k_i -th row of decorrelating matrix D, $(H)_{k_i}$ is the k_i -th column of the channel matrix. Besides ordering by SNR metric, in order to increase the performance system [5] proposed the SINR metric

$$(SINR)_{k_i} = \frac{\|(D)_{k_i} (H)_{k_i}\|^2 < |t_{k_i}|^2 >}{\sum_{k_j=1, k_j \neq k_i}^{n_r} \|(D)_{k_i} (D)_{k_j}\|^2 < |t_{k_j}|^2 > + \sigma_n^2 \|(D)_{k_i}\|^2} \quad (11)$$

The signal to noise and interference of the k_i -th sub-stream to be detected must be maximized.

IV. EFFECT OF MODIFIED CHANNEL MATRIX ON MMSE CRITERION

When nulling in the MMSE criterion, interference is not nulled absolutely as a trade-off between noise increase and interference decrease is considered. In ZF criterion, at the k_i -th detection stage because of the orthogonal property between $(D)_{k_i}$ and $(H)_{k_i}$ we have the result below

$$\begin{aligned} (D)_{k_i} r &= (D)_{k_i} (Ht + n) = \\ &= (D)_{k_i} Ht + (D)_{k_i} n = \alpha t + (D)_{k_i} n \end{aligned} \quad (12)$$

where $\alpha = [0, 0, \dots, 1, \dots, 0]$. The one value appears at k_i -th position and the remaining is zero. On

the contrary, in the MMSE the nulling operation is not complete hence the value α is given as

$$\alpha = [\alpha_{k_1}, \alpha_{k_2}, \dots, \alpha_{k_i}, \dots, \alpha_{k_j}, \dots, \alpha_{k_{nT}}]$$

where $\alpha_{k_j} \neq 0$. It means that interferences appear

at the k_i sub-stream. The main idea here is to reduce as many interference as possible. After detecting k_{i-1} sub-stream the channel matrix is deflated in a way that the k_{i-1} -th column is zero.

It is clear that the k_{i-1} -th element of $(D)_{k_i}$ is also zero. As a result, the product α between $(D)_{k_i}$ and $(H)_{k_i}$ is found as

$$\alpha = [0, 0, \dots, 0, \alpha_{k_i}, \dots, \alpha_{k_j}, \dots, \alpha_{k_{nT}}]$$

In conclusion, the interference from the detected sub-stream is suppressed. These above steps can be summarized as follow

Initialization

$$k_i \leftarrow 1$$

Recursion

$$D = (H^H H + \alpha_n^2 I_{n_r})^{-1} H^H$$

$$y_{k_i} = (D)_{k_i} r$$

$$t_{k_i} = Q(y_{k_i})$$

$$r = r - t_{k_i} (H)_{k_i}$$

$$(H)_{k_i} = 0$$

$$k_{i+1} \leftarrow k_i$$

V. COMPUTER SIMULATION RESULTS

In the simulation, we investigate the bit error rate (BER) for a V-BLAST system with $n_T = 4$ transmit and $n_R = 4$ receive antennas deploying uncoded BPSK modulation in all cases. Fig. 2 shows the performance of optimal order ZF and MMSE with and without modified channel matrix. The impact of modified channel matrix can be seen very clearly. MMSE Metric 1 (SINR maximum) gives nearly the same performance compared to ZF case. However when we apply the modified channel matrix into MMSE the BER much more is improved. Metric 1 with modified channel matrix results in a performance improvement of 6dB compared to optimal order ZF. Fig. 3 shows the performance of the MMSE detection algorithm in all cases. Without modified channel matrix Metric 1 (SINR maximum) and Metric 2 (SNR maximum) have nearly the same performance. But with modified channel matrix the Metric 1 has the best BER and the difference can be seen obviously.

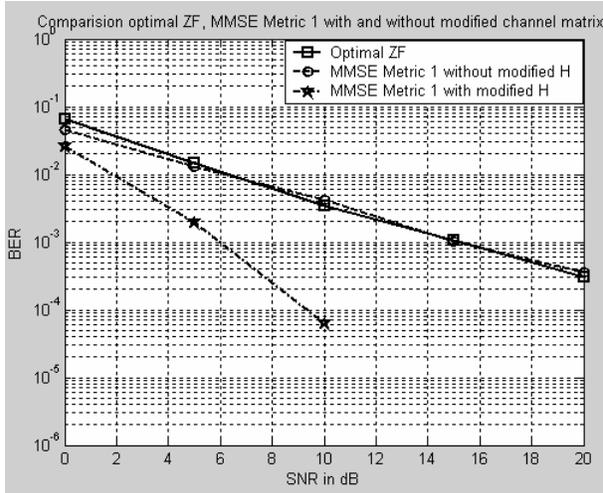


Fig. 2 Simulation with $n_T = 4, n_R = 4$ uncoded BPSK symbols

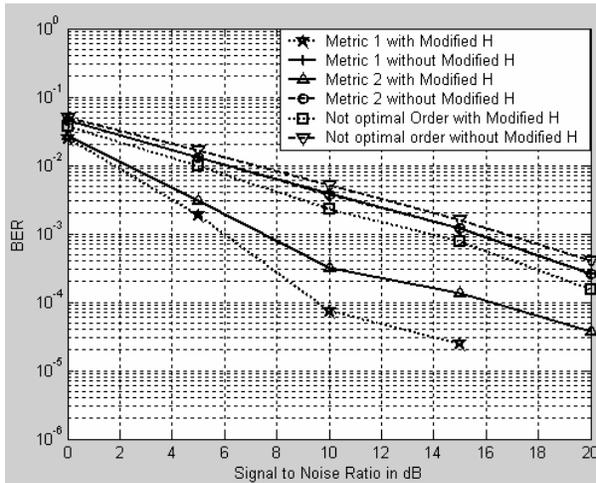


Fig. 3 Simulation MMSE algorithm in all cases with $n_T = 4, n_R = 4$ uncoded BPSK symbols

VI. CONCLUSION AND DISCUSSION

We have described the influence of modified channel matrix on system performance. Absolutely the BER performance is improved very much

because the interference of detected sub-stream is suppressed at the next stage. We also presented simulation results for several scenarios. This proposal can generally be used to in any kind of algorithm.

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