

# Improved B-Spline Contour Fitting Using Genetic Algorithm for the Segmentation of Dental Computerized Tomography Image Sequences

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**Abstract.** In the dental field, 3D tooth modeling, in which each tooth can be manipulated individually, is an essential component of the simulation of orthodontic surgery and treatment. However, in dental computerized tomography slices teeth are located closely together or inside alveolar bone having an intensity similar to that of teeth. This makes it difficult to individually segment a tooth before building its 3D model. Conventional methods such as the global threshold and snake algorithms fail to accurately extract the boundary of each tooth. In this paper, we present an improved contour extraction algorithm based on B-spline contour fitting using genetic algorithm. We propose a new fitting function incorporating the gradient direction information on the fitting contour to prevent it from invading the areas of other teeth or alveolar bone. Furthermore, to speed up the convergence to the best solution we use a novel adaptive probability for crossover and mutation in the evolutionary program of the genetic algorithm. Segmentation results for real dental images demonstrate that our method can accurately determine the boundary for individual teeth as well as its 3D model while other methods fail. Independent manipulation of each tooth model demonstrates the practical usage of our method. © 2007 Society for Imaging Science and Technology.

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## INTRODUCTION

The accurate 3D modeling of the mandible and the simulation of tooth movement play an important role in preoperative planning for dental and maxillofacial surgery. The 3D reconstruction of the teeth can be used in virtual reality based training for orthodontics students and for preoperative assessment by dental surgeons. For 3D modeling tooth segmentation to extract the individual contour of a tooth is of critical importance. Automated tooth segmentation methods from 3D digitized images have been researched for the measurement and simulation of orthodontic procedures.<sup>1</sup> These methods provide interstices along with their locations and orientations between the teeth for segmentation result. However, it does not give individual tooth contour information which manifests more details that are helpful in dental study. A thresholding method, used in the existing segmentation and reconstruction systems, is known to be efficient for automatic hard tissue segmentation.<sup>2,3</sup> Some morphological filtering methods are used for creating intermediary slices by interpolation for modeling teeth in 3D.<sup>4</sup> The morphological operations are also combined with the threshold-

ing method for dental segmentation in x-ray films.<sup>2</sup> However, neither the thresholding method nor the morphological filtering method is suitable for separating individual tooth regions using tooth computerized tomography (CT) slices, because some teeth touch each other and some are located inside of alveolar bone with a CT slice intensity profile similar to teeth.<sup>5</sup> A modified watershed algorithm was suggested to create closed-loop contours of teeth while alleviating the over-segmentation problem of the watershed algorithm.<sup>5</sup> Although this reduces the number of regions significantly, it still produces many irrelevant basins that make it difficult to define an accurate tooth contour. A seed-growing segmentation algorithm<sup>6</sup> was suggested based on B-spline fitting for arbitrary shape segmentation in sequential images. The best contour of an object is determined by fitting the initial contour passed by previous frame to the edges detected in the current frame. For the fitting operation, the objective function defined by the sum of distances between the initial contour and the object edges is used. For this algorithm to work properly, the complete object boundary should be extracted by global thresholding and the object should be located apart from other objects. If other objects are located nearby as in the case of the tooth CT image, the shape of the initial contour should be very close to the actual object contour to prevent being fitted to the boundaries of the nearby objects.

Many snake algorithms have been proposed for medical image analysis applications.<sup>7-10</sup> However, in the CT image sequence where objects are closely located, the classical snake algorithms have not yet been successful due to difficulties in initialization and the existence of multiple extrema. It is only successful when it is initialized close to the structure of interest and there is no object which has similar intensity values to those of interest.<sup>7</sup> The snake models for object boundary detection search for an optimal contour that minimizes (or maximizes) an objective function. The objective function generally consists of the internal energy representing the properties of a contour shape and the external potential energy depending on the image force. The final shape of the contour is influenced by how these two energy terms are represented. However, many snakes tend to shrink when its external energy is relatively small due to the lack of image

95 forces.<sup>7</sup> Some snakes also suffer from the limited flexibility of  
 96 representing the contour shape and a large number of de-  
 97 rivative terms in their internal energy representation. A  
 98 B-spline based snake has been developed as a B-spline snake  
 99 and B-snake to enhance the geometric flexibility and opti-  
 100 mization speed by means of a small number of control  
 101 points instead of snaxels.<sup>11,12</sup> B-spline snake controls con-  
 102 tour shapes by a stiffening parameter as well as its control  
 103 points, and detects object boundaries in noisy environments  
 104 by using gradient magnitude information instead of edge  
 105 information. This algorithm introduces a stiffening factor to  
 106 the B-spline function<sup>13</sup> that varies the spacing between the  
 107 spline knots and the number of sampled points used during  
 108 the evaluation of the objective function. In addition, the  
 109 factor controls the smoothness of curve and reduces the  
 110 computation of the cost function. Although the algorithm  
 111 was proposed to extract the contour of a deformable object  
 112 in a single image, it can be applied to the tooth segmentation  
 113 in CT slices. However, in tooth CT data, the algorithm may  
 114 cause the contour of a tooth to expand to include contours  
 115 of nearby teeth and alveolar bone, or it may cause the con-  
 116 tour to be contracted to a small region.

117 A B-spline fitting algorithm employing a genetic algo-  
 118 rithm (GA) was used to overcome local extrema indwelling  
 119 in the vicinity of an object of interest.<sup>14-17</sup> In this case, it was  
 120 shown that the GA does not require exhaustive search while  
 121 avoiding high-order derivatives for curve fitting or matching  
 122 problems.<sup>18,19</sup> However, the conventional GA-based B-spline  
 123 fitting still suffers from the influence of other objects and  
 124 often fails to extract the object boundary from the image  
 125 sequences when similar objects are adjacent to each other.

126 In this paper, we propose an improved B-spline contour  
 127 fitting algorithm using a GA to generate a smooth and ac-  
 128 curate tooth boundary for the 3D reconstruction of a tooth  
 129 model. We devise a new B-spline fitting function by incor-  
 130 porating the gradient direction information on the fitting  
 131 contours to search the tooth boundary while preventing it  
 132 from being fitted to neighboring spurious edges. We also  
 133 present an evolution method to accelerate the search speed  
 134 by means of automatic and dynamic determination of GA  
 135 probabilities for crossover and mutation. Experimental re-  
 136 sults show that our method can successfully extract the in-  
 137 dividual tooth boundary, compared with other methods  
 138 which fail to do so.

### 139 BACKGROUND

140 Dental CT images have the following two distinct character-  
 141 istics: (1) An individual tooth often appears with neighbor-  
 142 ing hard tissues such as other teeth and alveolar bone, and  
 143 (2) these neighboring hard tissues have the same or similar  
 144 intensity values to the tooth of interest. Thus, the fixed  
 145 threshold value for each tooth in each slice is not effective as  
 146 shown in Figure 1. When we try to obtain a tooth region by  
 147 thresholding method, the lower and upper limits of a thresh-  
 148 old value can be displayed at each slice for a given tooth by  
 149 the two curves in Fig. 1. Any threshold value within the limit  
 150 produces the tooth region with the accuracy better than

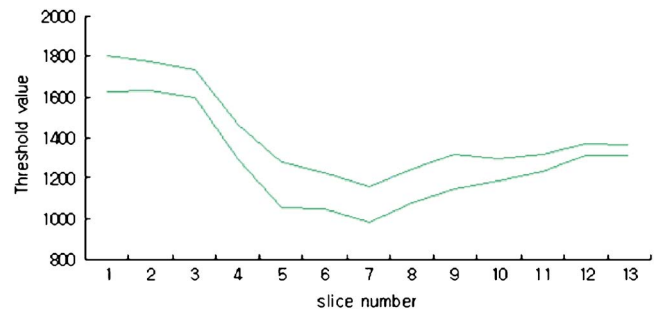


Figure 1. Threshold values for a certain tooth computed at different slices by manual.

90%. It shows us that individual segmentation method is  
 required for each tooth in each slice.

There are many segmentation methods, each of which  
 have their own limitations in separating individual tooth  
 regions on CT images.<sup>3-6</sup> An optimal thresholding scheme<sup>20</sup>  
 can be attempted by taking advantage of the fact that the  
 shape and intensity of each tooth changes gradually through  
 the CT image slices.

However, even if an optimal threshold is determined for  
 every slice, the result of the segmentation is found unsatis-  
 factory because of neighboring hard tissue. For the 3D re-  
 construction of an individual tooth model, the tooth bound-  
 ary needs to be defined more precisely.

### B-Spline Contour Fitting

The B-spline curve has attractive properties for the represen-  
 tation of an object contour with arbitrary shape. They are  
 also suitable for the curve fitting process and are summa-  
 rized as follows.

- An object of any shape, including those subsuming an-  
 gular points, can be represented by a set of control  
 points, a knot sequence, and a basis function. The shape  
 of the contour can be adjusted by simply repositioning  
 the control points in many fitting problems where the  
 knot sequence and basis function can be fixed.
- Little else remains to be different in the shape of the  
 contour by deducting the number of control points  
 within some tolerable limit for the purpose of reducing  
 information needed for fitting process. This allows the  
 fitting process to be faster with fewer variables over  
 which to optimize.

We choose the uniform cubic closed B-spline curve,  
 shown as follows in Eqs. (1) and (2), to describe the object  
 contours in the image:

$$\mathbf{r}(s) = \begin{bmatrix} r_x(s) \\ r_y(s) \end{bmatrix} = \begin{bmatrix} \sum_{i=0}^{n-1} x_i B_0(s-i) \\ \sum_{i=0}^{n-1} y_i B_0(s-i) \end{bmatrix}, \quad (1)$$

185 
$$B_0(s) = \begin{cases} |s|^3/2 - s^2 + 2/3 & \text{if } t_0 \leq |s| < t_1, \\ (2 - |s|)^3/6 & \text{if } t_1 \leq |s| < t_2, \\ 0 & \text{otherwise.} \end{cases} \quad (2)$$

186 In the equations,  $r(s)$  represents the coordinate of a contour  
 187 pixel at a specific value of parameter  $s$  and  $(x_i, y_i)$  represents  
 188 coordinates of  $i$ th control point. The B-spline basis func-  
 189 tions are translated copies of  $B_0(s)$ . In the case of tooth  
 190 segmentation we use a closed uniform knot sequence, as  
 191  $\{t_0, t_1, \dots, t_n\} = \{0, 1, \dots, n\}$  and  $t_0 = t_n$  where  $n$  is the total  
 192 number of the control points.

193 The B-spline fitting function  $f$  is represented in Eq. (3)  
 194 (Ref. 11) as follows:

195 
$$f = \sum_{k=0}^{M-1} |\nabla I[r(s_k)]|, \quad (3)$$

196 where  $M$  is the total number of contour points. The fitting  
 197 function is maximized when the contour conforms to the  
 198 object boundary. The B-spline fitting function makes use of  
 199 only external force computed based on the gradient magni-  
 200 tude on the contour. The smoothness constraint is implicitly  
 201 represented by the B-spline itself.

202 **B-spline Contour Fitting using Genetic Algorithm**

203 The genetic algorithm is a probabilistic technique for search-  
 204 ing for an optimal solution. The optimal solution is de-  
 205 scribed by a vector, called a “chromosome,” which can be  
 206 obtained by maximizing a fitting function. Hence the defi-  
 207 nition of the fitting function significantly affects the solution  
 208 state. A sequence of evolutionary operations is repeated for a  
 209 chromosome to evolve to its final state. The end of the evo-  
 210 lutionary operation is determined by checking the fitness  
 211 values, which represent the goodness of each chromosome in  
 212 the population.

213 A chromosome is a collection of genes, and a gene rep-  
 214 resents the control point of B-spline. Since the chromosome  
 215 represents a complete contour and a gene uses the actual  
 216 location of a control point, the search algorithm has neither  
 217 ambiguity on the contour location nor potential bias to par-  
 218 ticular shapes. To reduce the size of a gene, we use the index  
 219 value as a gene, instead of two coordinate values.<sup>16,17</sup> Com-  
 220 posing a search area based on the indices provides a search  
 221 area with arbitrary shape, where it is confined to search for  
 222 the final position of the control point to be found out. This  
 223 scheme of chromosome guarantees that gene information  
 224 does not spread over the chromosome, which results in short  
 225 length and order of schema.<sup>16</sup> Accordingly, there is a high  
 226 probability to converge fast. A new generation is made  
 227 through the sequence of evolutionary operations and, during  
 228 the evolutionary processes, crossover and mutation steps af-  
 229 fect the quality and speed of final solution significantly.

230 **IMPROVED B-SPLINE CONTOUR FITTING USING  
 231 GENETIC ALGORITHM**

232 **Fitting Function Based on Gradient Magnitude and  
 233 Direction**

234 The fitting function measures the fitness of the possible con-  
 235 tour to the object boundary in the current slice. The fitness

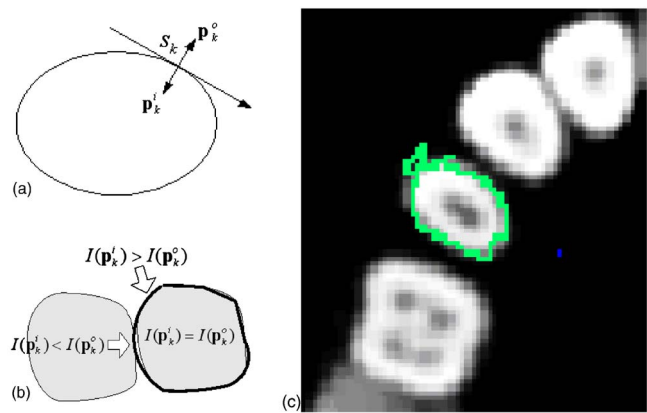


Figure 2. (a) Definition of inner and outer regions. (b) Illustration for fitting function—right object is of interest, with adjacent left object, and thick black curve is a fitting curve. (c) Twisted contour.

value is the basis for determining the termination of the  
 evolutionary process and selecting elite chromosomes for  
 mating pool generation. In the existing active contour mod-  
 els, the fitting function consists of the internal forces con-  
 trolling the smoothness of the contour and the external force  
 used for representing the object boundary information in  
 the image.<sup>7,12</sup> One drawback of this representation is that it  
 requires the determination of the weight values balancing  
 these two components.

B-spline snake makes use of a simple fitting function  
 with only external force computed based on the gradient  
 magnitude on the contour. The internal force terms are re-  
 placed by using a stiffening parameter and implicit smooth-  
 ness constraint of the B-spline representation of a contour.  
 However, in the image data such as the tooth CT image  
 slices, those fitting functions often generate the contour fit-  
 ted to the boundary of nearby object. They also generate the  
 contour contracted to a small region unless the stiffening  
 parameter is set properly.

Note that the magnitude of the intensity difference may  
 vary between the inside and outside of an object contour.  
 However, if the relative intensity between two sides of a con-  
 tour is maintained throughout the contour, the sign of the  
 intensity difference made by two sides is inverted when the  
 contour expands out to the boundary of another object.  
 Hence, when fixing moving direction of parameter  $s$  along  
 the curve, we are able to have knowledge of which side is  
 inside (or outside) in advance. This enables us to know  
 whether the contour is fitted to the object of interest or other  
 adjacent objects. In this paper, the fitting function to be  
 maximized is designed to take advantage of this property of  
 the data. This gradient direction information allows the fit-  
 ness function to penalize the portion of a contour fitted to  
 the neighboring object.

To compute the fitness value for a possible solution (or  
 chromosome), we first generate the contour points from the  
 B-spline representation of the solution and trace the contour  
 as shown in Figure 2(a). At the  $k$ th contour point  $r(s_k)$ , a  
 unit normal vector  $\mathbf{n}(s_k)$  is computed. Next, the inner region  
 and outer region pixel location  $\mathbf{p}_k^i$  and  $\mathbf{p}_k^o$ , respectively, are

276 identified by using  $\mathbf{n}(s_k)$  computed at the  $k$ th point  $\mathbf{r}(s_k)$   
 277 according to

$$278 \quad \mathbf{p}_k^o = \mathbf{r}(s_k) + \mathbf{n}(s_k) \quad (4)$$

279 and

$$280 \quad \mathbf{p}_k^i = \mathbf{r}(s_k) - \mathbf{n}(s_k). \quad (5)$$

281 Then, the fitness value is determined based on gradient  
 282 magnitude and direction information,  $\nabla_k$ , at each contour  
 283 point according to

$$284 \quad f = \sum_{k=0}^{M-1} (\nabla_k - \alpha_k), \quad (6)$$

285 where

$$286 \quad \nabla_k = \begin{cases} |\nabla I[\mathbf{r}(s_k)]| & \text{if } I(\mathbf{p}_k^i) - I(\mathbf{p}_k^o) > 0, \\ -|\nabla I[\mathbf{r}(s_k)]| & \text{if } I(\mathbf{p}_k^i) - I(\mathbf{p}_k^o) \leq 0, \end{cases}$$

287 and

$$288 \quad \alpha_k = \begin{cases} C, & \mathbf{r}(s_k) = \mathbf{r}(s_j) \\ 0, & \mathbf{r}(s_k) \neq \mathbf{r}(s_j) \end{cases}, \forall j \in \{0, 1, \dots, M-1\} \wedge j \neq k.$$

289  $I(\mathbf{p}_k^i)$  and  $I(\mathbf{p}_k^o)$  are intensity values of the inside and outside  
 290 of the  $k$ th contour point, respectively. This equation is fur-  
 291 ther illustrated by Fig. 2(b), where some portion of the con-  
 292 tour attaches to another object and in this portion  $I(\mathbf{p}_k^i)$   
 293  $< I(\mathbf{p}_k^o)$ , so we assign the negative gradient magnitude to  
 294 penalize the fitness value. The figure also shows that in other  
 295 portions the contour correctly conforms to the tooth bound-  
 296 ary and in these portions  $I(\mathbf{p}_k^i) > I(\mathbf{p}_k^o)$ , so we assign the  
 297 positive gradient magnitude to the fitness value. Note that  
 298 when there is no difference of gradient direction, which may  
 299 happen if inner and outer pixel values are identical, then  
 300  $I(\mathbf{p}_k^i) = I(\mathbf{p}_k^o)$ . This aims at preventing the contour from being  
 301 misfitted when the contour lies inside an object region hav-  
 302 ing uniform intensity values, such as the inside region of a  
 303 tooth.

304 A constant-valued penalty  $C$  is deducted from the fit-  
 305 ness value when the contour is twisted as shown in Fig. 2(c).  
 306 Our experimental results showed that setting the penalty too  
 307 high hindered searching the contour maximizing the sum of  
 308 gradient magnitudes. The proposed fitting method yields the  
 309 best performance when  $C$  is set to around 0.1% of the sum  
 310 of gradient magnitudes.

### 311 Improved Adaptive Evolutionary Operations

312 The evolutionary process generates a new population of pos-  
 313 sible solutions through the following three genetic operators:  
 314 reproduction (or selection), crossover, and mutation. The  
 315 selection operation constructs the mating pool from the cur-  
 316 rent population for the crossover operation. The results pre-  
 317 sented here use a tournament selection scheme.<sup>16</sup> The cross-  
 318 over operation generates two child chromosomes by  
 319 swapping genes between the two parent chromosomes. In  
 320 this paper we present one point cutting scheme by improved

adaptive crossover probability. We also use an adaptive mu-  
 321 tation probability scheme for our evolutionary process. 322

323 The conventional GA generally uses fixed crossover and  
 324 mutation probabilities. Adaptive genetic algorithm<sup>21</sup> (AGA)  
 325 was proposed by Srinivas et al. that uses variable crossover  
 326 and mutation probabilities that are determined automati-  
 327 cally based on fitness values during fitting process for fast  
 328 convergence rate. The probabilities for evolution are, there-  
 329 fore, no longer required to be set to constants. At the begin-  
 330 ning stage of the fitting process, we consider all the possi-  
 331 bilities of control point locations in the search area. As the  
 332 process goes on, we obtain the evolutionary probabilities  
 333 such that the possible solution near the optimal solution  
 334 quickly converges to the actual solution. In AGA,<sup>21</sup> the cross-  
 335 over probability is adaptively determined depending on the  
 336 fitness value  $f$ , according to

$$337 \quad p_c = \begin{cases} k_1 \frac{f_{\text{best}} - f}{f_{\text{best}} - f_{\text{avg}}}, & f \geq f_{\text{avg}}, \\ k_2, & f < f_{\text{avg}}, \end{cases} \quad (7)$$

338 where  $f_{\text{best}}$  and  $f_{\text{avg}}$  are the best and average fitness values in  
 339 the mating pool, respectively, and  $k_1$  and  $k_2$  are constants  
 340 and set to 1.0. Hence, if  $f = f_{\text{best}}$  when  $f \geq f_{\text{avg}}$ ,  $f$  is preserved,  
 341 although the value of  $k_1$  ensures high occurrence of cross-  
 342 over. If  $f < f_{\text{avg}}$ , crossover is operated without exceptions,  
 343 since its corresponding chromosome has low fitness value. 344

345 The mutation operation is also implemented by using  
 346 the mutation probability  $p_m$  as follows:

$$347 \quad p_m = \begin{cases} k_3 \frac{f_{\text{best}} - f}{f_{\text{best}} - f_{\text{avg}}}, & f \geq f_{\text{avg}}, \\ k_4, & f < f_{\text{avg}}, \end{cases} \quad (8)$$

348 where  $k_3$  and  $k_4$  are constants set to 0.5. As in the case of  
 349 crossover, the mutation operation does not affect the chro-  
 350 mosome with the best fitness value. However if  $f \leq f_{\text{avg}}$  its  
 351 mutation operation takes place with the most ambiguity  
 352 since  $k_3 = 0.5$ . 353

354 In this paper we propose an improved adaptive cross-  
 355 over probability. To maintain the solution with high fitness  
 356 value, we generate a random number  $p_r$  and consider the  
 357 relationship of  $p_r$  with  $p_{c1}$  and  $p_{c2}$ , where  $p_{c1}$  and  $p_{c2}$  denote  
 358 crossover probabilities generated from two parent chromo-  
 359 somes, father chromosome and mother chromosome respec-  
 360 tively. When two parent chromosomes are selected, two chil-  
 361 dren are generated as follows. 362

- 363 (1) Generate a random number  $p_r$  between 0 and 1 to  
 364 determine the adaptive crossover probability, gener-  
 365 ate a random number  $p_l$  between 0 and 1 to deter-  
 366 mine the crossing site, and generate a random  
 367 number  $p_s$  between 0 and 1 to determine which  
 side of the crossing site the portion of the chromo-  
 some should exchange with the corresponding por-  
 tion of its mate.

- 368 (2) Replace  $f$  in Eq. (7) by the fitness value of each  
 369 parent for computing the crossover probabilities,  
 370  $p_{c1}$  and  $p_{c2}$ .  
 371 (3) If  $p_r > p_{c1}$  and  $p_r > p_{c2}$ , put the two parents to the  
 372 next generation without change.  
 373 (4) If  $p_r$  is between  $p_{c1}$  and  $p_{c2}$ , thus  $p_{c1} \geq p_{c2}$  and  $p_s$   
 374  $< 0.5$  then the left portion of the father chromo-  
 375 some should be exchanged with the corresponding  
 376 portion of the mother chromosome to generate one  
 377 child and put mother chromosome directly to the  
 378 generation as another child. If  $p_s \geq 0.5$  then the  
 379 right portion from the father chromosome should  
 380 be exchanged to generate one child and another  
 381 child is a copy of the mother chromosome. Simi-  
 382 larly if  $p_{c1} < p_{c2}$  then the mother chromosome  
 383 should be changed and put to the next generation  
 384 while the father chromosome is put to the next  
 385 generation without any change. In addition, the  
 386 crossover scheme is determined by the value of  $p_s$ .  
 387 (5) If  $p_r$  is less than both  $p_{c1}$  and  $p_{c2}$ , generate two child  
 388 chromosomes as the normal crossover method  
 389 does.

390 In the proposed operation, the chromosomes with high  
 391 fitness values can survive until a new chromosome with  
 392 higher fitness is created. It supports rapid searching for an  
 393 optimal solution by taking advantage of the crossover  
 394 scheme swapping either side to the crossing site.

### 395 EXPERIMENTAL EVALUATION

396 We tested the proposed contour segmentation with two  
 397 kinds of sets of data: synthetic images and two sets of real  
 398 dental CT image sequences with a slice thickness of 0.67mm  
 399 and 1mm and  $x$ - $y$  resolution of  $512 \times 512$ . Visual C++ with  
 400 DICOM libraries<sup>22</sup> for reading 16-bit CT images and the 3D  
 401 graphics library OpenGL were used as tools to implement  
 402 the proposed algorithm. CT images are saved in DICOM  
 403 format, an international standard for medical images, after  
 404 acquisition through the commercially available Shimadzu  
 405 Ltd. SCT-7800 CT scanner. The test data were prepared to  
 406 reveal the capability of the proposed algorithm in finding an  
 407 accurate boundary among many similar objects nearby. We  
 408 compared the proposed algorithm with the existing B-spline  
 409 snake algorithm that uses the gradient magnitude based ex-  
 410 ternal force in the fitting function.<sup>11</sup>

411 First, we applied these algorithms to a synthetic image  
 412 similar to a tooth surrounded by alveolar bone. To generate  
 413 the results, we constructed a B-spline contour with 8 control  
 414 points and selected 20 initial chromosomes for each  $40$   
 415  $\times 40$  window. For the following examples of B-spline snake  
 416 the stiffening parameter is set to 2. As shown in Figure 3, the  
 417 proposed algorithm extracts an accurate object boundary  
 418 while the existing B-spline snake fails.

419 We also applied the two algorithms to real CT image  
 420 sequences where an individual tooth often appears with  
 421 neighboring hard tissues such as other teeth and alveolar  
 422 bone. If too many control points are used for a contour, it  
 423 reduces the smoothing effect on the curve and consequently

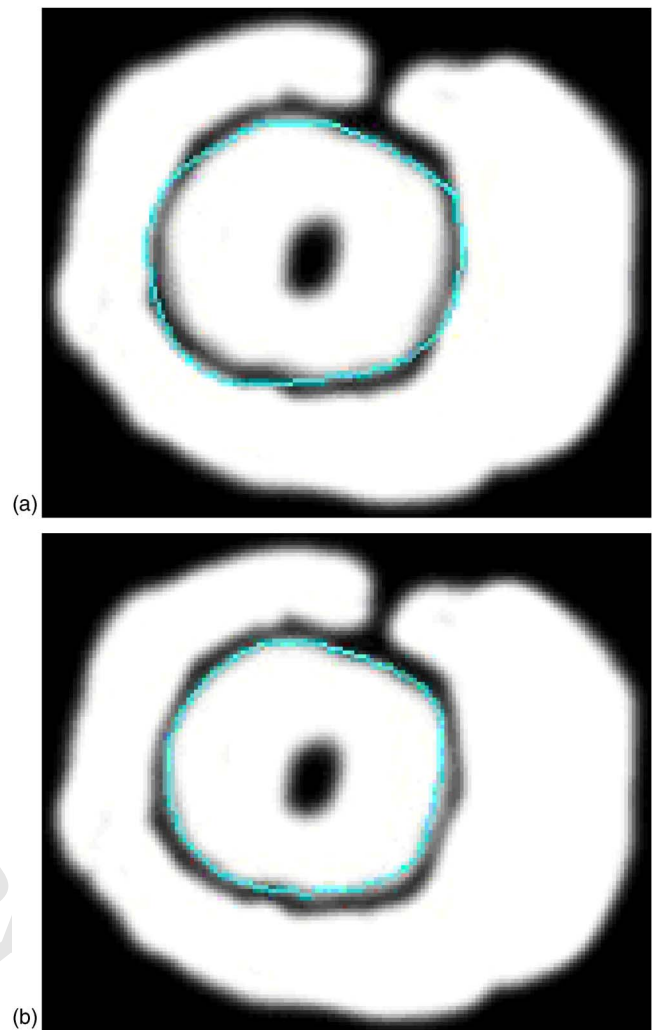


Figure 3. Contours extracted from the synthetic data (number of control points  $CP=8$ ). (a) By B-spline snake method. (b) By the proposed method.

424 generates twisted parts of contour as shown in Figure 4.  
 425 Figure 5 shows part of test results using different set of slices,  
 426 which have lower resolution. Since the test image is small, a  
 427  $10 \times 10$  search area suffices for a control point.

428 As shown in Fig. 5, an individual tooth often appears  
 429 with neighboring hard tissues such as other teeth and alveolar  
 430 bone, and the proposed algorithm produces better results  
 431 than B-spline snake. The difference in the results stems from  
 432 the fitting function.

433 Part of the segmentation results of slice sequences is  
 434 shown in Figure 6 and those of a molar having a more  
 435 complicated shape are shown in Figure 7. In Fig. 6, the fig-  
 436 ures at the far left side show the results of teeth initialization  
 437 for the first slice by applying a proper threshold to each  
 438 tooth interactively. As the segmentation is performed slice by  
 439 slice, in contrast with the results of proposed method, malfit-  
 440 ting error contained in the results of the existing method  
 441 increases.

442 Table I lists part of the numerical results of the segmen-  
 443 tation.  $N$  is the number of slices over which each tooth  
 444 spans. FPE (false positive error) is the percent of area re-

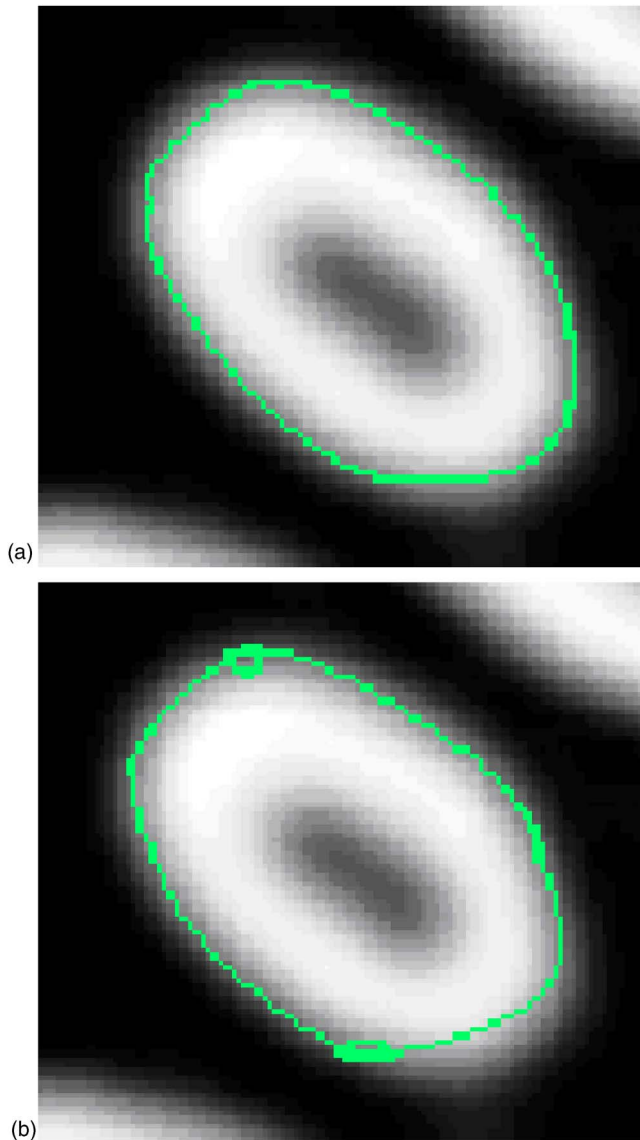


Figure 4. Tooth contours extracted from CT image ( $CP=16$ ). (a) By the proposed method. (b) By B-spline snake.

445 ported as a tooth by the algorithm, but not by manual seg-  
 446 mentation. FNE (false negative error) is the percent of area  
 447 reported by manual segmentation, but not by the algorithm.  
 448 Similarity and dissimilarity indices,<sup>23,10</sup> which show the  
 449 amount of agreement and disagreement,  $S_{agr}$  and  $S_{dis}$ , re-  
 450 spectively, between the algorithm area  $A_{alg}$  and the manual  
 451 segmentation area  $A_{man}$ , are computed according to

$$S_{agr} = 2 \frac{A_{man} \cap A_{alg}}{A_{man} + A_{alg}}, \quad (9)$$

$$S_{dis} = 2 \frac{A_{man} \cup A_{alg} - A_{man} \cap A_{alg}}{A_{man} + A_{alg}}. \quad (10)$$

454 These indices are calculated for validation on  $N$  slices of  
 455 each tooth. Averaged values of  $S_{agr}$  as well as its minimum  
 456 and maximum values are shown in Table I, and we conclude

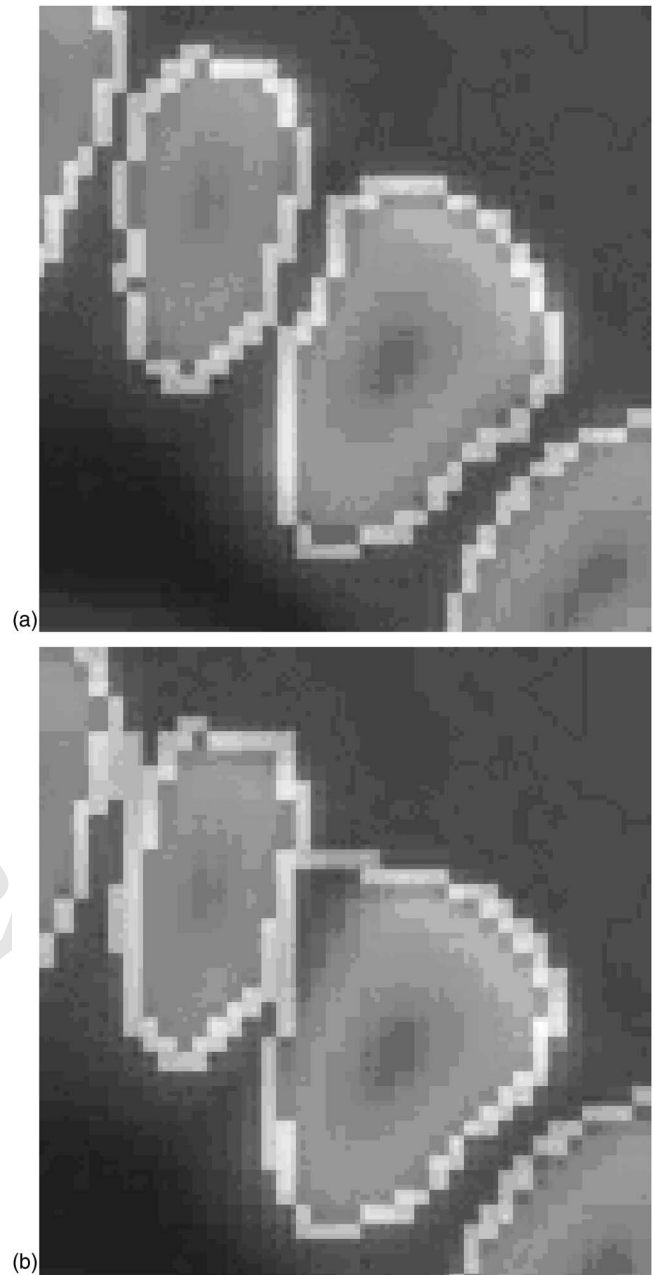


Figure 5. Tooth contours extracted from CT image sequence ( $CP=8$ ). (a) By the proposed method. (b) By B-spline snake.

that the proposed method for segmentation isolates individual region of tooth successfully, in contrast with the results of B-spline snake shown in Table II.

The proposed fitting method is designed for the fast contour extraction by the improved crossover method which uses a random number for copying genes of a superior chromosome to an inferior one when the random number falls into the range of crossover probabilities of its parents,  $p_{c1}$  and  $p_{c2}$ . Furthermore, the proposed crossover method decides which part of crossing site will be exchanged between parent chromosomes. The decided part fosters chromosomes to be competent with a high fitness value. We implement two genetic B-spline fittings with existing crossover methods to analyze the performance of the proposed cross-

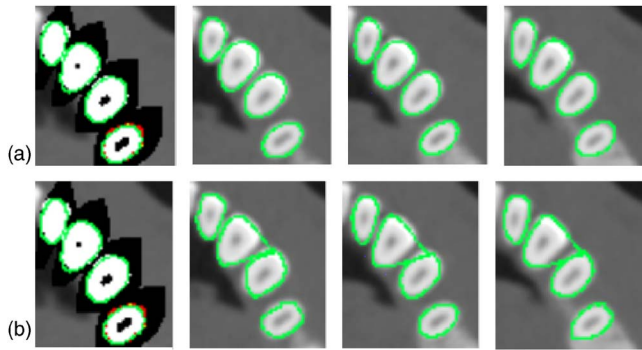


Figure 6. Tooth contours extracted from CT image sequence ( $CP=16$ ). (a) By the proposed method. (b) By B-spline snake.

Table I. Segmentation results for 8 teeth of the proposed method from the same scans of CT set.

Tooth	$N$	FPE[%]	FNE[%]	$S_{agr}$	$S_{min}$	$S_{max}$	$S_{dis}$
1	20	4.43	8.37	0.935	0.915	0.977	0.131
2	22	7.88	3.45	0.945	0.916	0.973	0.111
3	25	8.96	4.48	0.935	0.901	0.968	0.131
4	24	8.46	6.47	0.926	0.905	0.970	0.148
5	27	5.81	8.29	0.929	0.917	0.967	0.143
6	26	2.07	7.05	0.953	0.923	0.971	0.094
7	25	5.21	3.79	0.955	0.927	0.976	0.089
8	23	5.69	1.42	0.965	0.932	0.983	0.069

Table II. Segmentation results for 8 teeth of B-spline snake from the same scans of CT set.

Tooth	$N$	FPE[%]	FNE[%]	$S_{agr}$	$S_{min}$	$S_{max}$	$S_{dis}$
1	20	6.12	27.21	0.814	0.574	0.952	0.373
2	22	26.01	1.16	0.879	0.628	0.956	0.241
3	25	45.86	11.28	0.756	0.316	0.897	0.487
4	24	29.89	4.59	0.842	0.764	0.941	0.313
5	27	28.06	8.06	0.836	0.726	0.933	0.328
6	26	15.09	8.81	0.884	0.818	0.948	0.232
7	25	27.98	5.03	0.852	0.755	0.936	0.296
8	23	10.12	3.89	0.932	0.771	0.972	0.136

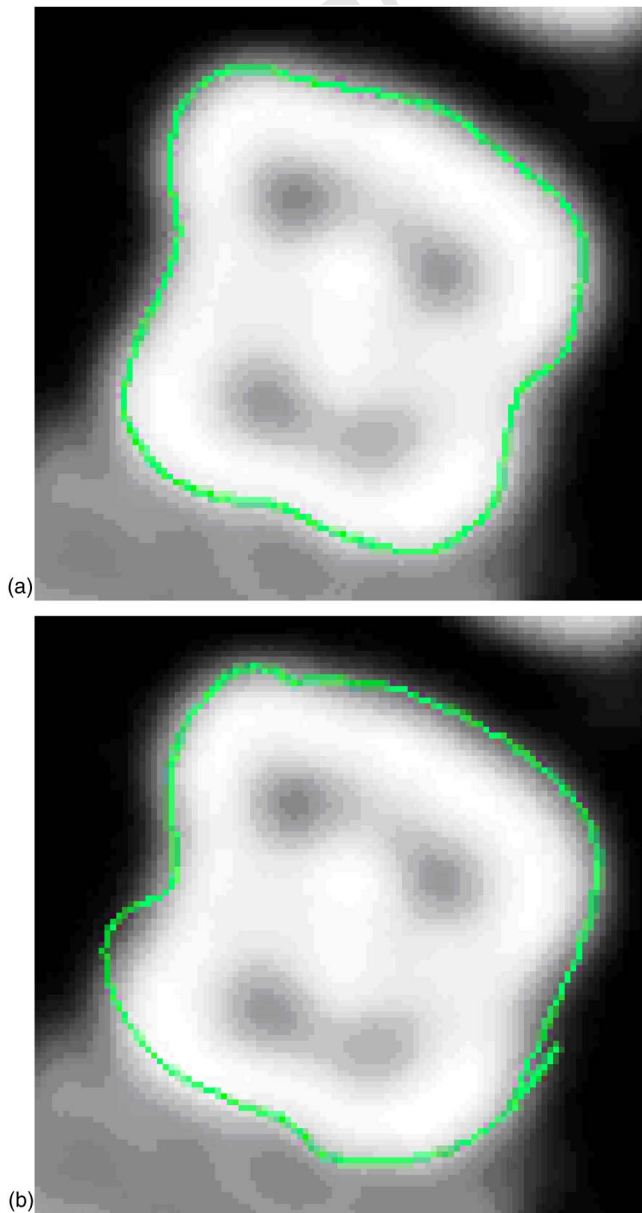


Figure 7. Extracted contours of molar ( $CP=32$ ). (a) By the proposed method. (b) By B-spline snake.

over. Both existing methods generate the initial population randomly, with uniform distribution, while using different crossover methods. “Method A” uses a fixed  $p_c$  of 0.75 and “Method B” uses AGA, which determines  $p_c$  adaptively. Figure 8 compares the convergence rate of the proposed crossover method with those of the existing methods in terms of the fitness value along chromosome generation. The figure shows that the proposed crossover method results in a better convergence rate than either method A or B. The proposed crossover method preserves the chromosomes with high fitness for fast convergence and the results shows it is effective to randomly select either side to crossing site for improved crossover operation.

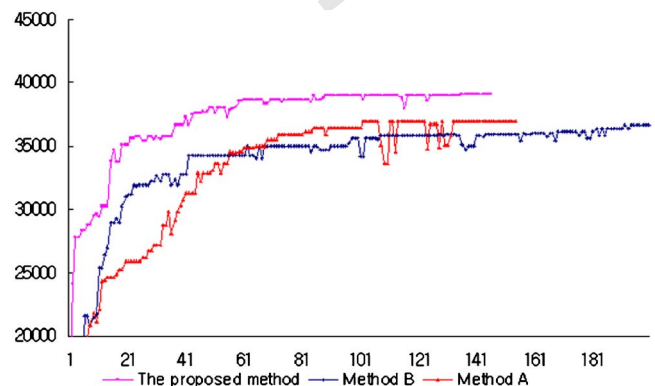


Figure 8. Comparison of convergence rates.

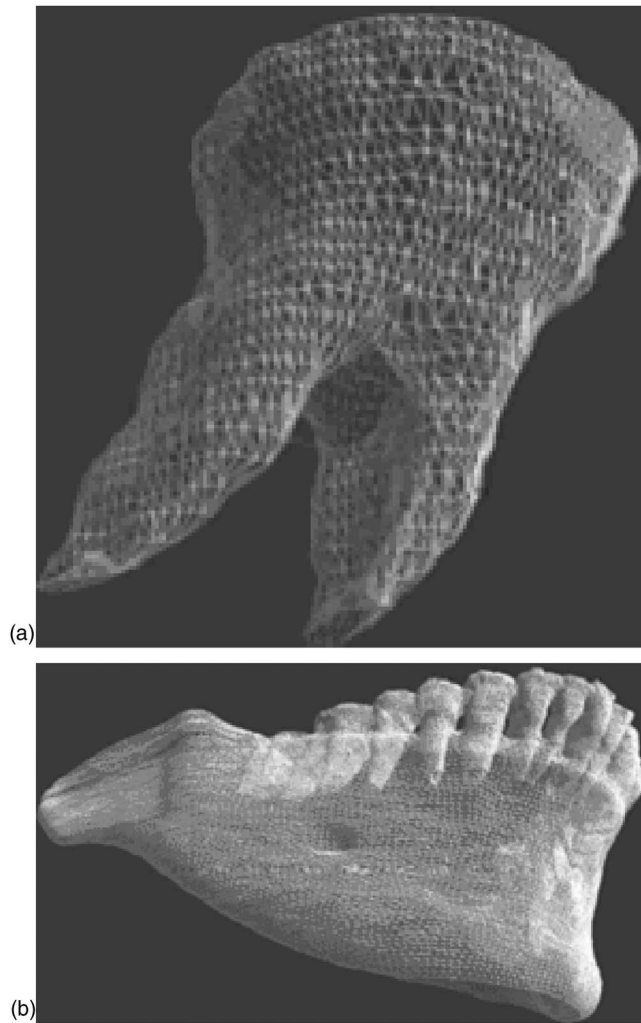


Figure 9. Wireframe models of tooth and mandible. (a) 3D reconstruction of tooth. (b) 3D reconstruction of mandible.

484 Individual segmentation of all teeth can be used to re-  
485 construct a model of the mandible, as shown in Figures 9  
486 and 10. Every tooth can be separated from the jaw for simu-  
487 lation of dental treatments.

#### 488 CONCLUSIONS

489 In this paper, we presented the improved genetic B-spline  
490 curve fitting algorithm for extracting individual smooth  
491 tooth contours from CT slices while preventing the contour  
492 from being twisted. This enables us to obtain individual ac-  
493 curate contours of teeth by overcoming the problem of the  
494 contour of a tooth expanding out to other teeth boundaries  
495 in the fitting process. Furthermore, we also devised the  
496 crossover method which accelerates convergence rate by  
497 means of both conserving chromosomes with high fitness  
498 value and allowing exchange of either side of cross site. The  
499 test results show that the proposed segmentation algorithm  
500 successfully extracts a smooth tooth contour under specific  
501 conditions such as the existence of objects in close vicinity.  
502 This paper also demonstrated the possibility of recon-  
503 struction of a 3D model in which each tooth was modeled  
504 and manipulated separately for the simulation of dental sur-

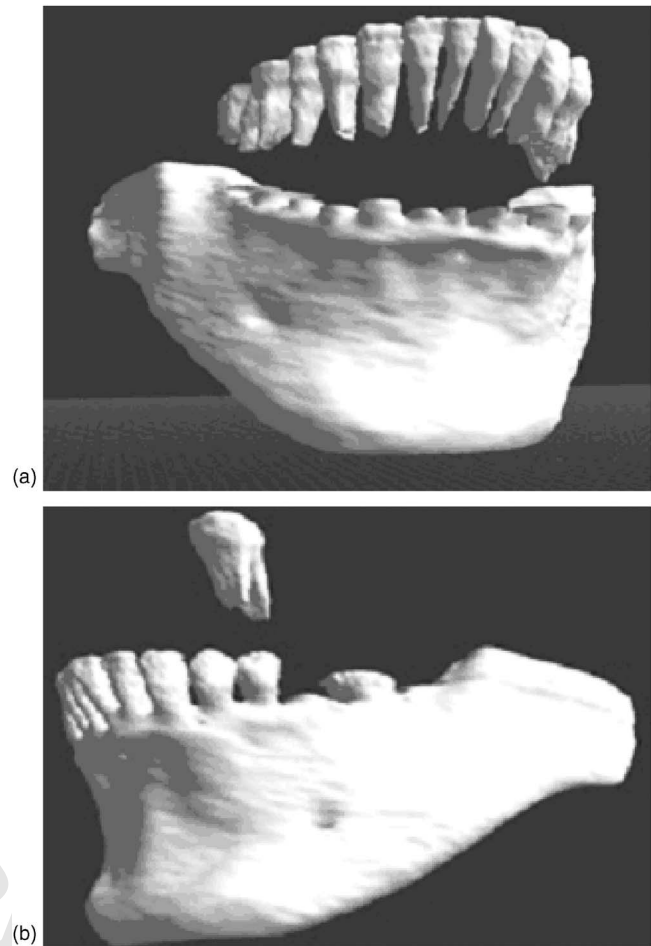


Figure 10. Manipulation of tooth. (a) Every tooth can be manipulated. (b) Simulation of having tooth out.

gery. These anatomical 3D models can be used for facilitat- 505  
ing diagnoses, pre-operative planning and prosthesis design. 506  
They will provide radiography of the mandible, an accurate 507  
mechanical model of the individual tooth and that of its root 508  
for endodontics and orthodontic operations. Hence the 3D 509  
reconstruction of the teeth can be used in virtual reality 510  
based training for orthodontics students and for preopera- 511  
tory assessment by dental surgeons. 512

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